ASSESSMENT OF DOSE EQUIVALENT DUE TO NEUTRINOS[†]

J. Donald Cossairt, Nancy L. Grossman, and Elaine T. Marshall*

Abstract—Neutrinos are present in the natural environment and are also produced by particle accelerators. A recent hypothesis has also been proposed that asserts that ionizing radiation due to neutrinos from certain astronomical events may have led to the extinction of some biological species. Thus, it is of interest to be able to estimate the dose equivalent due to these weakly interacting particles. Presented here are methods for estimating the dose equivalent due to neutrinos over a broad domain of energy, examples of such calculations, and an assessment of the postulated role of neutrinos in biological extinctions. It is concluded that the dose equivalent due to neutrinos from natural sources and from present-day accelerators is inconsequential and the postulated role of neutrinos in biological extinctions is highly improbable. Health Phys. 73(6):894-898; 1997

Key words: accelerators; dosimetry; dose assessment; radiobiology

INTRODUCTION

Neutrinos are present in the natural environment due to terrestrial, solar, and cosmic sources and are also produced at accelerators both incidentally and intentionally as part of physics research programs. Progress in fundamental physics research has led to the creation of beams of neutrinos of ever-increasing intensity and/or energy. The large size and cost associated with these beams attracts, and indeed requires, public interest, support, and some understanding of the "exotic" particles produced, including the neutrinos. Furthermore, the very word neutrino ("little neutral one," as coined by Enrico Fermi) can possibly lead to public concern due to confusion with "neutron," a word widely associated with radiological hazards. Adding to such possible concerns is an assertion, widely publicized, that neutrinos from astronomical events may have led to the extinction of some biological species. Presented here are methods for conservatively estimating the dose equivalent due to neutrinos as well as an assessment of the possible role of neutrinos in biological extinction processes.

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NEUTRINO INTERACTIONS AND DOSE EQUIVALENT/FLUENCE CONVERSION FACTORS

Neutrinos are neutral leptons, conventionally believed to be massless, that interact with matter solely through the weak interaction with very small cross sections. The Standard Model of Electroweak Interactions of Weinberg, Salam, and Glashow (Langacker and Erler 1996), highly successful in explaining these interactions, underlies the work presented in this section. There are three known "flavors" of neutrinos (ν 's) and their corresponding antiparticles (antineutrinos, $\overline{\nu}$'s) so that there are six types of these particles altogether: the electron neutrino and antineutrino $(\nu_e, \overline{\nu}_e)$, the muon neutrino and antineutrino $(\nu_{\mu}, \overline{\nu}_{\mu})$ and the tau neutrino and antineutrino $(\nu_{\tau}, \overline{\nu}_{\tau})$. Electron and muon neutrinos and antineutrinos have been extensively studied experimentally while tau neutrinos and antineutrinos have yet to be directly observed. Hence, the properties of the latter are correspondingly less well-known.

In the present work, a tissue composition is assumed that includes all elements present in the whole body at the level exceeding 1% by weight [hydrogen (10.1%), carbon (23.2%), nitrogen (2.6%), oxygen (61.6%), phosphorus (1.1%), and calcium (1.4%)] and whole body density, ρ , of 1.07 g cm⁻³ (ICRP 1975). The average number densities of the atomic electrons, nucleons, and nuclei can be calculated: $\rho_{\rm electrons} = 3.54 \times 10^{23} \ {\rm cm}^{-3}$, $\rho_{\rm nucleons} = 6.44 \times 10^{23} \ {\rm cm}^{-3}$, and $\rho_{\rm nuclei} = 4.60 \times 10^{22} \ {\rm cm}^{-3}$. The averages of atomic number, $Z_{\rm ave}$, neutron number, $N_{\rm ave}$, and atomic weight, $A_{\rm ave}$, are 7.048, 6.959, and 14.007, respectively. The whole body is approximated by a tissue slab 30 cm thick. In the remainder of this section, four processes involving neutrino interactions with matter are considered.

Process A: Neutrino scattering from atomic electrons

Electrons recoiling from elastic scattering of neutrinos deposit energy in tissue. The cross section for this process, $\sigma_{\nu\text{-electron}}$, has been presented by Langacker and Erler (1996) and Bahcall (1989) as

$$\dot{\sigma_{\nu-\text{electron}}} = CE_{\nu} \times 10^{-45} (\text{cm}^2), \tag{1}$$

where, $C(\nu_e) = 9.2$, $C(\overline{\nu}_e) = 3.9$, $C(\nu_\mu) = 1.6$ and $C(\overline{\nu}_\mu) = 1.3$ with E_ν , the neutrino energy, in MeV. The maximum recoil kinetic energy, $T_{\rm max}(E_\nu)$, that can be

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^{*} Fermi National Accelerator Laboratory, P. O. Box 500, Batavia, IL 60510.

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transferred by a massless particle of energy E_{ν} in an elastic collision with a particle of rest energy m_0c^2 is

$$T_{max} = \frac{2E_{\nu}^2}{m_o c^2 + 2E_{\nu}}. (2)$$

A reasonable estimate of the average value of the recoil kinetic energy, $T_{\rm ave}$, is $0.67T_{\rm max}$. Because of the large multiple scattering of the recoiling electrons, and the fact that their radiation quality factor is unity over a very large domain of energy, the dose equivalent/fluence, $P(E_{\nu})$, for the neutrinos can be calculated as follows, with $T_{\rm ave}$ in MeV:

 $P(E_{\nu})$

= 1.6 × 10⁻⁴
$$\sigma_{\nu-\text{electron}} T_{\text{ave}} \frac{\rho_{\text{electrons}}}{\rho}$$
 ($\mu S \nu \text{ cm}^2$). (3)

Process B: Neutrino scattering from nuclei

In this process, described by Drukier and Stodolsky (1984), the neutrinos interact with nuclei coherently. The process is strictly effective for low energies where the de Broglie wavelength of the neutrinos is too long to resolve individual nucleons. At higher energies, scattering from nucleons (see Processes C and D) gradually becomes more important. Here, the recoiling particles are low energy ions having large linear energy transfer (LET). $P(E_{\nu})$, using $N_{\rm ave}$ and $T_{\rm ave}$ (MeV), can be calculated according to:

 $P(E_{\nu})$

$$= 1.6 \times 10^{-4} \sigma_{\nu-\text{nucleus}} T_{\text{ave}} \frac{\rho_{\text{nuclei}}}{\rho} Q \quad (\mu S \nu \text{ cm}^2), \quad (4)$$

where $\sigma_{\nu\text{-nucleus}}$ is the cross section for this process. Q, the quality factor for these high LET ions, is conservatively taken to have the maximum value of 30 (ICRP 1991). The distribution of recoil energy over tissue volume due to the short (<<1 cm) ionization ranges of the recoil ions in tissue is taken to be uniform.

Where strict coherence applies, $\sigma_{\nu\text{-nucleus}}$ for ν 's is given by

$$\sigma_{\nu-\text{nucleus}} = 4.2 \times 10^{-45} N^2 E_{\nu}^2 \text{ (cm}^2),$$
 (5)

where E_{ν} is in MeV and N is the neutron number of the recoiling nucleus. These values were used in eqn (4) for $E_{\nu} \leq 20$ MeV. For $E_{\nu} > 20$ MeV, values of $\sigma_{\nu\text{-nucleus}}$ given by Boehm and Vogel (1992) for nuclei including those comprising tissue were used in eqn (4). This process is considered to be independent of flavor, but the cross sections for $\overline{\nu}$'s are approximately one half as large.

Process C: Neutrino scattering from nucleons-unshielded

For $50 \le E_{\nu} \le 200$ MeV, Boehm and Vogel (1992) give values of the total cross section, $\sigma_{\nu\text{-nucleon}}$, for scattering of ν 's from nucleons. Over this energy domain, this cross section is a monotonically-increasing function of energy and ranges from 4.0×10^{-41} to 5.5×10^{-41}

 10^{-40} cm². The corresponding cross section for $\overline{\nu}$'s is approximately one half as large. $P(E_{\nu})$ can be obtained from

$$P(E_{\nu}) = \sigma_{\nu-\text{nucleon}} F_{\text{nucleon}}(T_{\text{ave}}) R(T_{\text{ave}})$$

$$\rho_{\text{nucleons}}(\mu S v \text{ cm}^2), \quad (6)$$

where $R(T_{\rm ave})$ is the range of protons in tissue having a kinetic energy of $T_{\rm ave}$. R is taken to be 15 cm if the proton range exceeds 15 cm. The restriction $R \leq 15$ cm reflects the fact that the average neutrino will interact in the center of the tissue slab. $F_{\rm nucleon}(T_{\rm ave})$, in $\mu {\rm Sv~cm^2}$, is the dose equivalent/fluence factor of Schopper (1990) for nucleons of kinetic energy $T_{\rm ave}$, averaged over the equally probable recoils of protons and neutrons. The "straight-ahead approximation," which deposits the energy of the recoil in the same direction as the incident neutrino and overstates the forward-peaking of the recoils found at these energies, is used.

For $E_{\nu} \geq 0.5$ GeV, the interaction of neutrinos produces a number of secondary particles. This number, the multiplicity M, is a monotonically-increasing function of the center of mass energy, $E_{\rm CM}$, of the collision. For $0.5 < E_{\nu} < 10^4$ GeV, $1.66 < E_{\rm CM} < 137$ GeV. Over this domain of $E_{\rm CM}$ values of M have been tabulated by the Particle Data Group (1992) for leptonic (electron-positron) and hadronic (proton-antiproton) collisions. Since in this process, the scattering is "semi-leptonic," the averages of these two sets of values of M are used. M increases from 2 to 20 over this domain of E_{ν} . For these energies, $\sigma_{\nu\text{-nucleon}}$ (for neutrinos) and $\sigma_{\overline{\nu}\text{-nucleon}}$ (for antineutrinos) are given by the Particle Data Group (1992), with E_{ν} in GeV, as

$$\sigma_{\nu-\text{nucleon}} = 6.7 \times 10^{-39} E_{\nu} (\text{cm}^2).$$
 (7)

$$\sigma_{\nu-\text{nucleon}} = 3.4 \times 10^{-39} E_{\nu} (\text{cm}^2).$$
 (8)

For this process, $P(E_{\nu})$ is estimated also using the straight-ahead approximation:

$$P(E_{\nu}) = \sigma_{\nu-\text{nucleon}} M(E_{CM})$$

$$F_{\pi}[T_{ave}/M(E_{CM})]R\rho_{\text{nucleon}}(\mu Sv \text{ cm}^2),$$
 (9)

where F_{π} [$T_{\text{ave}}/M(E_{\text{CM}})$] is the dose equivalent/fluence factor of Schopper (1990) for positive pions (π^+ 's) at the average secondary particle energy. Thus, equal sharing of T_{ave} over the M secondary particles is assumed. The choice of π^+ 's to represent all of the secondary particles is conservative; alternative production of leptons (e.g., muons or electrons) would reduce the dose equivalent. This procedure benefits from the lack of strong dependence of F on hadron type or energy. R is again taken to be 15 cm to reflect the occurrence of the average interaction in the center of the tissues lab. The process is regarded as "flavor-blind," affecting all three flavors in the same manner. The approach taken to develop eqn(9) is valid for high energy neutrinos encountered by the tissue slab with essentially no material between the source of the neutrinos and the tissue slab. The more

common situation encountered, for example at particle accelerators, involves the presence of shielding material between the source of the neutrinos and the tissue slab (see Process D).

Process D: Neutrino scattering from nucleons-shielded

High energy neutrinos (e.g., those with $E_{\nu} \ge 0.5$ GeV) emerging from a thick layer of material (for example, earth shielding) and incident on the tissue slab result in a higher dose equivalent. This is due to the fact that the tissue slab in this situation is also exposed to secondary particles produced by neutrinos interacting in the shielding material. Many of these particles are hadrons, particles subject to the nuclear interaction. In a given non-gaseous material these hadrons have a characteristic mean free path on the order of tens of centimeters. It follows that after several meters of material, the absorbed dose and dose equivalent in the tissue slab and the absorbed dose in the intervening shielding reaches an equilibrium value. This value is, to good approximation, equivalent to that which would result if each of the neutrino interactions occurring in a unit mass of material were to deposit the entire neutrino energy, E_{in} in that mass.[‡] The approximation is improved if the neutrino flux density is uniform over a cross-sectional area larger than an exposed individual, a condition that generally holds both at accelerators and in nature. It will also hold for very long shields given the large values of mean free path for the neutrinos implied by the extremely small values of $\sigma_{\nu\text{-nucleon}}$. Thus, $P(E_{\nu})$ for neutrinos can be calculated as

$$P(E_{\nu}) = 0.16 \sigma_{\nu-\text{nucleon}} E_{\nu} N_A Q \quad (\mu S \nu \text{ cm}^2), \quad (10)$$

where E_{ν} is in GeV, $N_{\rm A}$ is Avogadro's number (the number of nucleons per unit mass), and Q is the quality factor appropriate for the secondary particles produced in these interactions. The secondary particles produced in such high energy neutrino interactions are generally energetic charged particles with few high energy neutrons present. A value of Q=1.3 is used as a conservative choice as it allows about one-third of these particles to be high energy neutrons. The dose equivalent calculated according to eqn (10) will naturally include that due to Process C.

Fig. 1 plots $P(E_{\nu})$ for the four processes for ν 's (as distinct from $\overline{\nu}$'s) along with the total value for all mechanisms considered. For process A, only the results for ν_{μ} 's are plotted for simplicity. For all other processes, the results for all ν 's are plotted.

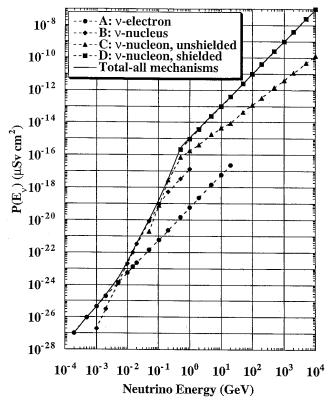


Fig. 1. Values of $P(E_{\nu})$, the dose equivalent/fluence, plotted as a function of neutrino energy, E_{ν} for the four processes described in the text. The sum for all four mechanisms is also plotted for ν_{μ} 's. The results calculated for Process A for ν_{μ} 's are plotted. Processes B, C, and D are regarded as "flavor blind." Values for antineutrinos are smaller, see text. The symbols on the curves are at the coordinates where the individual calculations were performed.

APPLICATIONS TO SPECIFIC CALCULATIONS

Solar neutrinos

Bahcall (1989) has elegantly described the current understanding of the neutrinos emitted by the Sun. He gives the predicted total neutrino flux density of these neutrinos at the Earth of 6.6×10^{10} cm⁻² s⁻¹. These neutrinos are all ν_e 's. The dominant process by which the Sun emits neutrinos is that in which two protons interact to produce ²H ("pp neutrinos"). This process results in a flux density on Earth of approximately 6×10^{10} cm⁻² s⁻¹ and has a maximum of E_{ν} of approximately 0.42 MeV. The neutrinos produced in the part of the thermonuclear reaction chain involving ⁸B ("⁸B neutrinos") have a maximum of E_{ν} of approximately 15 MeV. On Earth, the flux density of these neutrinos is approximately 5.8×10^6 cm⁻² s⁻¹. One can calculate the dose equivalent due to the solar neutrinos, assuming they all reach the Earth. § For the pp neutrinos, Process A dominates, especially when one corrects the values in Fig. 1 to

^{*} N. Mokhov, personal communication, Fermi National Accelerator Laboratory, P.O. Box 500, Batavia, Illinois February 21, 1997.

This phenomenon may be understood by its analogy to the electronic equilibrium often discussed in connection with instrumentation designed to measure "exposure" due to photons.

 $^{^\$}$ To date, experiments have found the flux densities of $\nu_{\rm e}$'s to be less than these predicted values. This is the famous "solar neutrino problem" (Boehm and Vogel 1992; Bahcall 1989).

 v_e 's (instead of v_μ 's) to obtain $P=2.9\times 10^{-26}~\mu Sv$ cm², assuming the maximum neutrino energy. Inserting the flux density, a dose equivalent rate, $dH/dt=1.7\times 10^{-15}~\mu Sv$ s⁻¹ = 5.5 × $10^{-8}~\mu Sv$ y⁻¹ is calculated. For the ⁸B neutrinos, both Processes A and B contribute. Assuming all neutrinos to have the maximum nenergy, Process A gives a value of $P=7.2\times 10^{-23}~\mu Sv$ cm² (again, calculating the value for v_e 's) while for Process B, $P=1.0\times 10^{-22}~\mu Sv$ cm². Thus, the total is $P=1.72\times 10^{-22}~\mu Sv$ cm², resulting in $dH/dt=1.0\times 10^{-15}~\mu Sv$ s⁻¹ = 3.1 × $10^{-8}~\mu Sv$ y⁻¹. Thus, for all solar neutrinos, dH/dt is approximately $10^{-7}~\mu Sv$ y⁻¹ on Earth.

Estimate for the Fermilab neutrinos at the main injector project (NuMI)

The U.S. Department of Energy is considering the construction of a new beam of neutrinos $(\nu_{\mu}$'s) at Fermilab which would be directed through the crust of the Earth over a distance of about 800 km toward an existing proton decay experiment at Soudan, Minnesota. The goal is to see if any of the ν_{μ} 's become ν_e 's or ν_{τ} 's over their flight and, if so, demonstrate that neutrinos have a small, nonzero mass (Boehm and Vogel 1992). The designed beam of ν_{μ} 's has an average energy of 13 GeV so that only Process D is important. Calculations of the flux density of neutrinos in the center of this beam as a function of distance from the production target have been performed. Using eqn (10), which yields $P(E_{\nu}) = 1.64 \times 10^{-13} \, \mu \text{Sv cm}^2$, the dose equivalent rates shown in Table 1 are calculated.

EXTINCTION OF SPECIES

Collar (1996) has presented a hypothesis that the final stages of stellar collapse could have led to the extinction of some species on earth due to the interaction of the neutrinos produced by these cosmic events. This theory has appeared, sometimes sensationally, in public media. Collar observed that the neutrinos emitted by such events would be in the energy regime dominated by Process B. Noting the high LET of the recoiling nuclei, Collar concluded that these neutrinos could have caused the mass extinctions known from paleontology. Collar calculated the spectrum of neutrinos and determined their fluence as a function of distance from the collapse. Assuming tissue to be C₄H₄₀O₁₇N, he calculated an average absorbed dose due to one of these collapses of 10^{-8} Gy at 3.09×10^{13} km (1 parsec or 3.26 light years). Given the chosen tissue composition, oxygen recoils would be the most damaging because of their prevalence, the enhanced value of $\sigma_{\nu\text{-nucleus}}$ due to the N^2 factor in eqn (5), and their high LET ($\approx 257 \text{ keV } \mu\text{m}^{-1}$). Collar deduced that as many as 4 to 12 malignant foci kg⁻¹ in tissue on earth would occur due to collapses that might happen every 30 to 100 My. This result is based upon an estimate that the average recoil results in interactions

Table 1. Results of calculations of dose equivalent for the proposed NuMI neutrino beam at Fermilab.

Distance from target	Neutrino flux density	Dose equivalent rate
(km)	$(cm^{-2} y^{-1})$	$(\mu \text{Sv y}^{-1})$
1	7.6×10^{13}	1.2×10^{1}
90	3.4×10^{9}	5.6×10^{-4}
550	1.0×10^{8}	1.7×10^{-5}
730	5.2×10^{7}	8.5×10^{-6}

with 3.6 nucleosomes out of 3×10^7 per cell nucleus and assumes that only one hit is required to result in malignancy. He concluded that large mass species, of relatively low populations, might have sufficient members killed by the tumors to result in nonviable populations. Smaller, more populous organisms might survive.

Several questions have been raised concerning this hypothesis (Cossairt and Marshall 1997). Collar cites results principally from in vitro studies. The connection of results from such studies to in vivo conditions with respect to specific end points presents problems that were not considered by Collar. Such problems have been discussed, e.g., by Turner and Fry (1994). References cited by Collar express conclusions, with suitable caveats, that unique and important biological effects may result from high (LET) radiation. The caveats, though not quoted by Collar, are important as exemplified by Goodhead (1988) who states, "Further understanding of these questions could lead, in future [sic], to substantial increases or decreases in estimations of risk." Recent studies that better define the boundaries of the effects of high LET radiation now exist.

Collar has referred to "effectively infinite" values of relative biological effectiveness (RBE). One can estimate a value of RBE for the radiation damage due to the recoils for fatal cancer. An established measure of risk for *Homo sapiens* exposed to photons is 5×10^{-2} latent fatal cancers Gy⁻¹ (ICRP 1991). If the absorbed dose of 10^{-8} Gy due to a stellar collapse were due to photons, the expected incidence rate of fatal cancers would be 5 × 10⁻¹⁰. For reference, humans are subject to a lifetime cancer mortality rate of about 20% (Cember 1983). It is thus unlikely that an increment of, say, 1% in this mortality rate would result in extinction. For 10⁻⁸ Gy due to the neutrino recoils to result in a fatal incidence rate of 0.01 (1%), the RBE would have to be approximately 2×10^7 . Accepted RBE values assigned for all end points inclusive of cancer induction, do not exceed approximately 200 (NCRP 1990). Specifically, values determined in recent work involving high LET ions are also bounded by this value, which is far smaller than needed to support Collar's conclusion (Scholz and Kraft 1994; Jenner et al. 1994; Kiefer et al. 1994; Edwards et al. 1994; Barendsen 1994).

CONCLUSION

Methods have been presented for calculating the dose equivalent due to neutrinos spanning a large range

[¶] These are exemplified by *The Boston Globe*, January 11, 1996, p. 13; *The New York Times*, January 23, 1996, p. B8; and *Scientific American*, April 1996, p. 20.

of energies. It is found that neutrinos produced by the Sun and present-day particle accelerators produce inconsequential dose equivalent rates. Examining recent calculations concerning neutrinos incident upon the Earth due to stellar collapse, it is concluded that it is highly unlikely that these neutrinos caused the mass extinctions of species found in the paleontological record.

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